

Problem 4: Show that if M is the set of all positive integers, then no point is a limit point of M .

Solution: Since M is the set of all positive integers, $M = \{1, 2, 3, 4, \dots\}$. Let there exist an open interval (a, b) containing the point n . $(a, b) = (n-1, n+1)$. So $n > n-1$ and $n < n+1$. Since $n-1$ and $n+1$ are endpoints of the open interval they are not included in the interval. This means n is the only point in open interval because there are no positive integers in between the points $n-1$ and n , and there are no points in between n and $n+1$. Therefore, no point of M is a limit point.