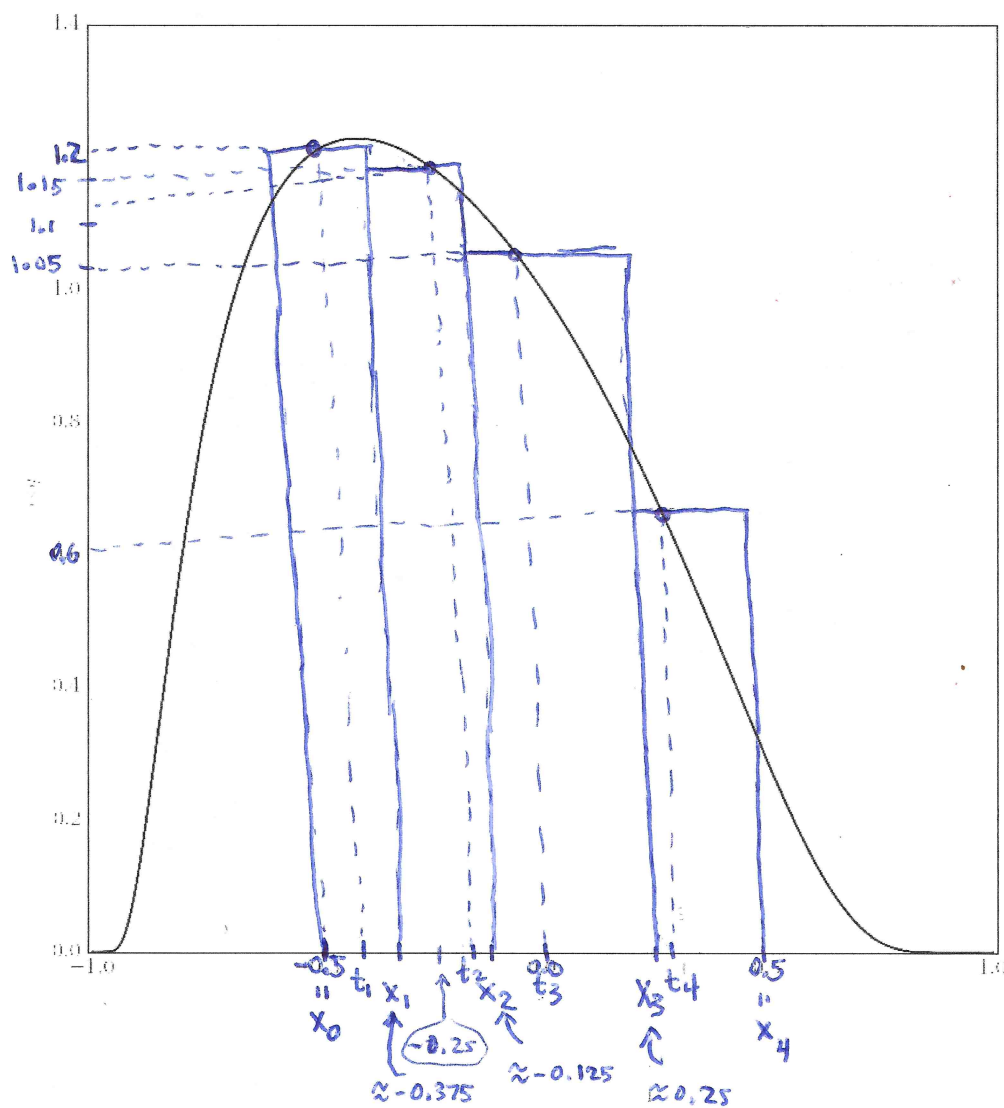


Homework 8 — MATH 4590 (Spring 2018)

1. The Euler phi function  $\phi: (-1, 1) \rightarrow \mathbb{R}$  is defined by  $\phi(x) = \prod_{k=1}^{\infty} (1 - x^k)$  (this is an "infinite product"). Estimate the value of the integral  $\int_{-0.5}^{0.5} \phi(x) dx$  using a Riemann sum with a partition pair  $P, T$  where  $P$  contains 5 total points (draw and label everything involved). A plot of the function is shown:



	Width	Height
Rect 1	0.125	1.2
2	0.25	1.15
3	0.375	1.05
4	0.25	0.6

$$P = \{x_0, x_1, x_2, x_3, x_4\}, T = \{t_1, t_2, t_3, t_4\}$$

$$R(\phi, P, T) = (0.125)(1.2) + (0.25)(1.15) + (0.375)(1.05) + (0.25)(0.6) = 0.98125$$