

Section 1.3 #140: Simplify the expression by writing it in terms of sines and cosines, then simplify: $\sec(x) \sin(x) \cot(x)$.

Solution: We know $\sec(x) = \frac{1}{\cos(x)}$ and $\cot(x) = \frac{\cos(x)}{\sin(x)}$. Plugging these in yields

$$\begin{aligned} \sec(x) \sin(x) \cot(x) &= \left(\frac{1}{\cos(x)} \right) \sin(x) \left(\frac{\cos(x)}{\sin(x)} \right) \\ &= \left(\frac{1}{\cos(x)} \right) \cancel{\sin(x)} \left(\frac{\cos(x)}{\cancel{\sin(x)}} \right) \\ &= 1. \end{aligned}$$

Section 1.3 #156: Solve the trigonometric equation on the interval $0 \leq \theta < 2\pi$:

$$1 + \cos(\theta) = \frac{1}{2}.$$

Solution: First isolate $\cos(\theta)$ here by subtracting 1 on both sides to get the equation $\cos(\theta) = -\frac{1}{2}$. To solve this means to look at the unit circle and find the angle θ that yields a point on the circle whose x -coordinate is $-\frac{1}{2}$. These are the points $\theta = \frac{2\pi}{3}$ and $\theta = \frac{4\pi}{3}$.