

5. (12 points) Suppose that the quantity supplied $S(p)$ and quantity demanded $D(p)$ where p denotes price in dollars of hot dogs at a baseball game are given by the following functions: $S(p) = -300 + 470p$ and $D(p) = 700 - 30p$.

(a) Find the equilibrium price for hot dogs at the baseball game. Show all your work for partial credit points!

$$\begin{aligned} S(p) &= D(p) \\ -300 + 470p &= 700 - 30p \\ 500p &= 1000 \\ p &= 2 \end{aligned}$$

(b) Using part (a), find the equilibrium quantity. Show all your work for partial credit points!

$$\begin{aligned} D(2) &= 700 - 30(2) \\ &= 700 - 60 \\ &= 640 \end{aligned}$$

6. (7 points) Find the midpoint between the following two points: $(-1, 1)$ and $(5, 7)$. Show all your work for partial credit points!

$$\begin{aligned} M((-1, 1), (5, 7)) &= \left(\frac{-1+5}{2}, \frac{1+7}{2} \right) \\ &= \left(\frac{4}{2}, \frac{8}{2} \right) = (2, 4) \end{aligned}$$

7. (7 points) Find the slope of $y = 7x + 3$ using two points on its graph and the slope formula. Show all your work for partial credit points!

Two points: $(1, 10), (0, 3)$

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{3-10}{0-1} = \frac{-7}{-1} = 7$$